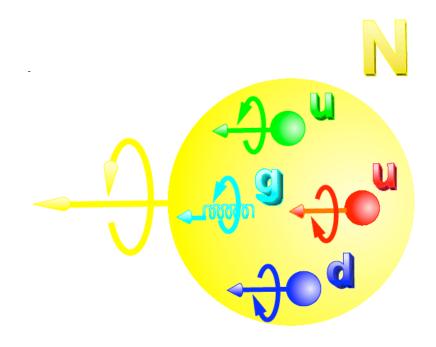
Today: let's look at spin in QCD

The nucleon, a composite particle with spin



## So, what carries the proton spin?

$$rac{\mathbf{1}}{\mathbf{2}} \; = \; \langle \mathbf{P}, rac{\mathbf{1}}{\mathbf{2}} | \; \mathbf{J_3} \; | \mathbf{p}, rac{\mathbf{1}}{\mathbf{2}} 
angle$$

$$\mathbf{J_i} \; = \; -rac{1}{2} \epsilon_{\mathbf{i}\mathbf{j}\mathbf{k}} \; \mathbf{M^{jk}} \; = \; \int \, \mathbf{d^3x} \; \left[ ec{\mathbf{x}} \, imes \, ec{\mathbf{T}_{\mathbf{QCD}}} 
ight]_{\mathbf{i}} \; .$$

## In QCD:

$$J_3 = \int d^3x \left[\underbrace{\bar{\psi}\,\gamma^3\gamma_5\,\psi}_{\sim \,\,\text{quark spin}} + \underbrace{\psi^\dagger\left(\vec{x}\times\left(-i\vec{\mathcal{D}}\right)\right)_3\psi}_{\sim \,\,\text{quark OAM}} + \underbrace{\left[\vec{x}\times\left(\vec{E}(\vec{x})\times\vec{B}(\vec{x})\right)\right]_3}_{\sim \,\,\text{total gluon ang. mom.}}\right]$$